Introduction
This document describes the usage of RL78 16bit-Fixed-point and Motor Control Library which is suitable for motor control S/W.

Target Device
RL78/G14 Group

Development environment
IDE Package: CubeSuite+ for RL78,78K V1.02.00
Compiler Package: CubeSuite+ RL78,78K0R Compiler CA78K0R V.1.4.0
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General Precautions in the Handling of MPU/MCU Products
1. Digital Signal Controller Library
The Digital Signal Controller library contains 2 key components of motor control libraries namely
16-bit Fixed-point
Motor Control

The above can be found commonly in Motor Control software. This application note aims to explain the usage of both components as 16-bit Fixed-point or 16-bit Fixed-point with Motor Control since Fixed Point can be used in any applications.

1.1 "r_stdint.h"
This header file defines the following basic integer types.

```c
typedef signed char int8_t;
typedef unsigned char uint8_t;
typedef signed short int16_t;
typedef unsigned short uint16_t;
typedef signed long int32_t;
typedef unsigned long uint32_t;
```
2. 16-bit Fixed-point Library

2.1 Overview
This library provides real-number operations using fixed-point format\(^1\) for RL78/G14 Group. This library is focusing a motor control library released from RENESAS, but this is also useful for other application areas.

The 16-bit fixed-point library enables fast real-number operations, especially on CPU's without FPU.

This library supports the following functions.
1. Multiplication and division
2. Mathematical functions (sin, cos, atan, and sqrt)
3. Conversion between floating point data.

Multiplication functions support for fixed-point type with 8, 10, 12, 14 or 16 fraction bits. Use 8-bit, 10-bit, 12-bit, 14-bit or 16-bit depending on the required precision of your application. The library functions mainly support 12-bit precision.

In fixed-point arithmetic, the range of values is restricted compared with floating point. So appropriate precision should be selected according to the input/output values of each operations.

2.2 Format of Fixed-point Data
Following is the format of fixed-point data supported in this library.

<table>
<thead>
<tr>
<th>15</th>
<th>14</th>
<th>n</th>
<th>n-1</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sign</td>
<td>Integer Part</td>
<td>Fraction Part</td>
<td></td>
<td></td>
</tr>
<tr>
<td>(1bit)</td>
<td>(16 - (1+n) bits)</td>
<td>(n bits)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

0: Positive
1: Negative

Figure 1. Fixed-point Data Format

According to the number of bits in fraction part, types FIX8, FIX10, FIX12, FIX14 and FIX16 are supported. The number indicates the number of bits in the fraction type.

Generic fixed-point type FIX is also supported, and generic fixed-point operations are supported for this type.

---

\(^1\) Fixed-point format represents a real number by assuming a decimal point at some fixed bit position.
2.3 Library Files

2.3.1 16-bit Fixed-point library only

The following include file and library files are provided.

When using this library alone, include the file indicated in table 1, and link the library file (corresponding to the compiler option) indicated in table 2.

<table>
<thead>
<tr>
<th>Library</th>
<th>Function</th>
<th>Library Files</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fixed-point library</td>
<td>Implements fixed-point operations</td>
<td><em>r_fixmath.h</em></td>
</tr>
</tbody>
</table>

Before using, copy these files into your local include or library directories.

```c
#include directory — r_fixmath.h, rstdint.h
library R_dsp_rl78.lib
```

Example of Usage

The following example shows a program using FIX12 operation and how to specify the library under CubeSuite+.

**Source Program**

```c
#include <stdio.h>
#include "r_fixmath.h" // Necessary when using
                      // fixed-point library

#define M_PI  (2048) /* pi */
#define M_2PI_3 (1365) /* 2*pi/3 */
#define M_PI_2  (1024) /* pi/2 */
#define M_PI_4  ( 512) /* pi/4 */

void print_sin()
{
  float r_flt;
  FIX12 r_fix12;
  
  r_fix12 = R_FIX_sin_int16(M_PI_2); // computes sin
  r_flt = FIX12_tofloat(r_fix12); // Convert back for printing
  printf("%f\n", r_flt);
}
```
Select [Property] of [CA78K0R] in project tree menu. In the dialog box [Property], select tab [Frequently Used Options (for Link)], and specify the library in "Using libraries" and the library path in "Additional library paths".

Figure 3. Specifying library
2.3.2 16-bit Fixed-point and Motor Control library

The following include file and library files are provided.

When using this library with motor control, include the file indicated in table 3, and link the library file (corresponding to the compiler option) indicated in table 4.

<table>
<thead>
<tr>
<th>Library</th>
<th>Function</th>
<th>Include File</th>
<th>Library File</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fixed-point library with motor control</td>
<td>Implements fixed-point and motor control operations</td>
<td>&quot;r_dsp.h&quot;</td>
<td></td>
</tr>
</tbody>
</table>

Table 3. Include File for Fixed-point Library

<table>
<thead>
<tr>
<th>Library name</th>
<th>Compiler Option</th>
</tr>
</thead>
<tbody>
<tr>
<td>R_dsp_rl78.lib</td>
<td>RL78/G14</td>
</tr>
</tbody>
</table>

Table 4. Fixed-point Libraries

Before using, copy these files into your local include or library directories.

```
#include r_dsp.h, rstdint.h
library       R_dsp_rl78.lib
```

Figure 3. Sample Configuration

**Example of Usage**

The following example shows a program using FIX12 operation with motor and how to specify the library under CubeSuite+.

```
#include <stdio.h>
#include "r_dsp.h" // Necessary when using fixed-point with motor library
#define M_PI  (2048) /* pi */
#define M_2PI_3 (1365) /* 2*pi/3 */
#define M_PI_2  (1024) /* pi/2 */
#define M_PI_4  ( 512) /* pi/4 */

void motor_uvw2dq()
{
  int16_t theta = 0;
  int16_t ia, ib;
  int16_t iu_ad, iw_ad;
  int16_t id_lpf, iq_lpf;

  while(1)
  {
    theta += M_PI_4;
    theta %= (2*M_PI);
    iu_ad = R_FIX_sin_int16(theta); //simulate iu
    iw_ad = R_FIX_sin_int16(theta + M_2PI_3); //simulate iw
    R_motor_uw2ab_int16( iu_ad, iw_ad, &ia, &ib );
    R_motor_ab2dq_int16( ia, ib, theta, &id_lpf, &iq_lpf ); //get feedback id and iq
    printf("%d\n", id_lpf);
    printf("%d\n", iq_lpf);
  }
}
```

[Source Program]
[How to specify the library under CubeSuite+]

Select [Property] of [CA78K0R] in project tree menu. In the dialog box [Property], select tab [Frequently Used Options (for Link)], and specify the library in "Using libraries" and the library path in “Additional library paths”.

Figure 3. Specifying library

2.4 Notes on Library Usage

If the result of operation or conversion exceeds the range of fixed-point type, the result is not guaranteed.
3. Specification of 16-bit Fixed-point Library

3.1 "r_fixmath.h"/"r_dsp.h"

This header file defines types and functions for fixed-point operations. Table 5 shows the types defined in the file and supported functions (macros).

NOTATION: The notation \(<n>\) in type, function, or macro names represents a number from 1 to 16. The number in the function or macro name corresponds to the number in the type name.

<table>
<thead>
<tr>
<th>Type</th>
<th>Supported functions and macros</th>
</tr>
</thead>
<tbody>
<tr>
<td>FIX8, FIX10, FIX12, FIX14, FIX16</td>
<td>R_FIX&lt;n&gt;_mul_int16, FIX&lt;n&gt;_tofloat, FIX&lt;n&gt;_fromfloat, FIX&lt;n&gt;_todouble, FIX&lt;n&gt;_fromdouble</td>
</tr>
<tr>
<td>FIX12</td>
<td>R_FIX_sin_int16, R_FIX_cos_int16, R_FIX_sqrt_int16, R_FIX_sqrt2_int16</td>
</tr>
<tr>
<td>int16_t / uint16_t</td>
<td>R_FIX_atan_int16, R_FIX_atan2_int16, R_FIX_limit_int16, R_FIX_ulimit_int16, R_FIX_div_int16</td>
</tr>
<tr>
<td>int32_t</td>
<td>R_FIX_mul32_int16</td>
</tr>
</tbody>
</table>

FIX8, FIX10, FIX12, FIX14, FIX16 and FIX are defined as short type.

When the operands and the result of an operation are the same type (FIX<n>), use the function corresponding to that type.

[Hints on Fixed-point Library Usage]

(1) Select one of the standard fixed-point type (FIX10 or FIX12) according to the requirement of your application.
(2) Compared with floating-point types, fixed-point types have limited range of values. It is recommended to select appropriate fixed-point types according to the range of input or intermediate result, or required precision of arithmetic.
(3) When converting data between different fixed-point types, use shift operator of C language.

Example: Conversion from FIX10 to FIX12

```c
FIX10 x, FIX12 y;
x=y>>2;
```

(4) When adding or subtracting between data of the same fixed-point type, use integer addition or subtraction of the C language.

Example: Addition of FIX12.

```c
FIX12 x, y, z;
z=x+y;
```

(5) Conversion between floating-point types and fixed-point types should be done only when required. Unnecessary conversions reduces the efficiency. But the conversion function applied to a constant generates a constant expression by expanding a macro, and fixed-point constant can be specified without any overhead.

Example: Fixed-point constant.

```c
FIX12 x;
x=FIX12_fromfloat(3.14f);
```
Table 6 shows the representations and ranges of fixed types.

<table>
<thead>
<tr>
<th>Type</th>
<th>Size</th>
<th>Alignment</th>
<th>Sign</th>
<th>Range</th>
<th>Minimum Value</th>
<th>Maximum Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>FIX8</td>
<td>2</td>
<td>2</td>
<td>signed</td>
<td>-2(-128.0)</td>
<td>2(^{-2}) (127.99609375)</td>
<td></td>
</tr>
<tr>
<td>FIX10</td>
<td>2</td>
<td>2</td>
<td>signed</td>
<td>-2(-32.0)</td>
<td>2(^{-2}) (31.999234375)</td>
<td></td>
</tr>
<tr>
<td>FIX12</td>
<td>2</td>
<td>2</td>
<td>signed</td>
<td>-2(-8.0)</td>
<td>2(^{-2}) (7.99755859375)</td>
<td></td>
</tr>
<tr>
<td>FIX14</td>
<td>2</td>
<td>2</td>
<td>signed</td>
<td>-2(-2.0)</td>
<td>2(^{-2}) (1.9993896484375)</td>
<td></td>
</tr>
<tr>
<td>FIX16</td>
<td>2</td>
<td>2</td>
<td>signed</td>
<td>-2(-0.5)</td>
<td>2(^{-2}) (0.4999847412109375)</td>
<td></td>
</tr>
</tbody>
</table>

The macros defined are listed in table 7.

<table>
<thead>
<tr>
<th>Category</th>
<th>Name</th>
<th>Parameter Type</th>
<th>Return Type</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Conversion</td>
<td>FIX&lt;n&gt;_tofloat</td>
<td>float</td>
<td>float</td>
<td>Converts FIX&lt;n&gt; to float.</td>
</tr>
<tr>
<td></td>
<td>FIX&lt;n&gt;_fromfloat</td>
<td>float</td>
<td>FIX&lt;n&gt;</td>
<td>Converts float to FIX&lt;n&gt;.</td>
</tr>
<tr>
<td></td>
<td>FIX&lt;n&gt;_todouble</td>
<td>FIX&lt;n&gt;</td>
<td>double</td>
<td>Converts FIX&lt;n&gt; to double.</td>
</tr>
<tr>
<td></td>
<td>FIX&lt;n&gt;_fromdouble</td>
<td>double</td>
<td>FIX&lt;n&gt;</td>
<td>Converts double to FIX&lt;n&gt;.</td>
</tr>
</tbody>
</table>

If the result of operation is outside the range of the data type, its value is not guaranteed.

The functions declared are listed in table 8.

<table>
<thead>
<tr>
<th>Category</th>
<th>Name</th>
<th>Parameter Type</th>
<th>Return Type</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Multiplication</td>
<td>R_FIX&lt;n&gt;_mul_int16</td>
<td>FIX&lt;n&gt;</td>
<td>FIX&lt;n&gt;</td>
<td>Computes multiplication of fixed-point data.</td>
</tr>
<tr>
<td></td>
<td>R_FIX_mul32_int16</td>
<td>int16_t</td>
<td>int32_t</td>
<td>Computes multiplication of 16-bit integer data.</td>
</tr>
<tr>
<td>Division</td>
<td>R_FIX_div_int16</td>
<td>uint16_t</td>
<td>uint16_t</td>
<td>Computes division of unsigned 16-bit integer data</td>
</tr>
<tr>
<td>Sine</td>
<td>R_FIX_sin_int16</td>
<td>FIX12</td>
<td>FIX12</td>
<td>Computes sine of fixed-oant data (radian)</td>
</tr>
<tr>
<td>Cosine</td>
<td>R_FIX_cos_int16</td>
<td>FIX12</td>
<td>FIX12</td>
<td>Computes cosine of fixed-point data (radian).</td>
</tr>
<tr>
<td>Arctangent</td>
<td>R_FIX_atan_int16</td>
<td>FIX&lt;n&gt;</td>
<td>FIX&lt;n&gt;</td>
<td>Computes the principal radian value of arctangent of fixed-point data.</td>
</tr>
<tr>
<td></td>
<td>R_FIX_atan2_int16</td>
<td>FIX&lt;n&gt;</td>
<td>FIX&lt;n&gt;</td>
<td>Computes the principal radian value of arctangent of y/x.</td>
</tr>
<tr>
<td>Square Root</td>
<td>R_FIX_sqrt_int16</td>
<td>uint16_t</td>
<td>uint16_t</td>
<td>Computes square root of fixed-point data</td>
</tr>
<tr>
<td></td>
<td>R_FIX_sqrt2_int16</td>
<td>int16_t</td>
<td>int16_t</td>
<td>Computes square root of x(^2) + y(^2)</td>
</tr>
<tr>
<td>Limit</td>
<td>R_FIX_limit_int16</td>
<td>int16_t</td>
<td>int16_t</td>
<td>Computes limited value</td>
</tr>
<tr>
<td></td>
<td>R_FIX_ulimit_int16</td>
<td>int16_t</td>
<td>uint16_t</td>
<td>Computes limited value greater than or equal to 0.</td>
</tr>
</tbody>
</table>

If the result of operation is outside the range of the data type, its value is not guaranteed.
3.2 Description of Functions

3.2.1 Conversion (macro)

(1) Conversion from float type to fixed-point

[Interface] FX<n> FIX<n>_fromfloat(float x)

n: 8,10,12,14,16

[Description] Converts float type data to fixed-point type.

[Header] "r_fixmath.h"

[Return Value] Result of conversion

[Parameters] x: Source of conversion

[Example]
#include "r_fixmath.h"
float x;
FIX12 ret;
ret = FIX12_fromfloat(x);

(2) Conversion from double type to fixed-point

[Interface] FX<n> FIX<n>_fromdouble(double x)

n: 8,10,12,14,16

[Description] Converts double type data to fixed-point type.

[Header] "r_fixmath.h"

[Return Value] Result of conversion

[Parameters] x: Source of conversion

[Example]
#include "r_fixmath.h"
double x;
FIX12 ret;
ret = FIX12_fromdouble(x);
(3) Conversion from fixed-point type to float

[Interface] float FIX<n>_tofloat(FIX<n> x)

n: 8, 10, 12, 14, 16

[Description] Converts fixed-point data to float.

[Header] "r_fixmath.h"

[Return Value] Result of conversion

[Parameters] x: Source of conversion

[Example]
```
#include "r_fixmath.h"

FIX12 x;
float ret;

ret = FIX12_tofloat(x);
```

(4) Conversion from fixed-point type to double

[Interface] double FIX<n>_todouble(FIX<n> x)

n: 8, 10, 12, 14, 16

[Description] Converts fixed-point data to double.

[Header] "r_fixmath.h"

[Return Value] Result of conversion

[Parameters] x: Source of conversion

[Example]
```
#include "fixmath.h"

FIX12 x;
double ret;

ret = FIX12_todouble(x);
```
3.2.2 Multiplication

(1) Multiplication of fixed-point data

**[Interface]** FIX<n> R_FIX<n>_mul_int16(FIX<n> x, FIX<n> y)

n: 8, 10, 12, 14, 16

**[Description]** Computes the multiplication of two fixed-point data of FIX<n> type. 32-bit intermediate result is used. Supposing fraction part both of x and y is n-bit, computes the product of two fixed-point data and the values of x and y are multiplied as long data, and shifted n bits to the right.

**[Header]** "r_fixmath.h"

**[Return Value]** Result of multiplication

**[Parameters]**
- x: Fixed-point data.
- y: Fixed-point data

**[Example]**
```
#include "r_fixmath.h"
FIX12 x, y, ret;
ret = R_FIX12_mul_int16(x, y);
```

(2) Multiplication of 16-bit integer data

**[Interface]** int32_t R_FIX_mul32_int16(int16_t x, int16_t y)

**[Description]** Computes the multiplication of two 16-bit integer data and computes the product of two data. The result is 32-bit integer data.

**[Header]** "r_fixmath.h"

**[Return Value]** 32-bit integer result of multiplication

**[Parameters]**
- x: 16-bit integer data.
- y: 16-bit integer data

**[Example]**
```
#include "r_fixmath.h"
int16_t x, y;
Int32_t ret;
ret = R_FIX_mul32_int16(x, y);
```
3.2.3 Division

[Interface] uint16_t R_FIX_div_int16(uint16_t a, uint16_t b)

[Description] Computes the value \((a \times 65536) / b\) and returns the quotient.

[Header] "r_fixmath.h"

[Return Value] The quotient of division

[Parameters] x: unsigned 16-bit integer data.
             y: unsigned 16-bit integer data

[Example]
#include "r_fixmath.h"
uint16_t x, y, ret;

    ret = R_FIX_div_int16(x, y);
### 3.2.4 Sine Function

**[Interface]** int16_t R_FIX_sin_int16 (int16_t x)

**[Description]** Computes the sine function of FIX12 fixed-point data (radian value). For given input "x", computes 4096 * \( \sin \left( \frac{2\pi \cdot x}{4096} \right) \)

**[Header]** "r_fixmath.h"

**[Return Value]** Result of sine in the FIX12 fixed-point data.

**[Parameters]**
- x: Fixed-point data (radian)

**[Example]**
```c
#include "r_fixmath.h"
FIX12 x, ret;

ret = R_FIX_sin_int16 (x);
```
3.2.5 Cosine Function

**[Interface]** int16_t R_FIX_cos_int16(int16_t x)

**[Description]** Computes the cosine function of FIX12 fixed-point data (radian value). For given input "x", computes $4096 \times \cos \left(\frac{2\pi \times x}{4096}\right)$

**[Header]** "r_fixmath.h"

**[Return Value]** Result of cosine in the FIX12 fixed-point data.

**[Parameters]** x: Fixed-point data (radian)

**[Example]**
```c
#include "r_fixmath.h"

FIX12 x, ret;

ret = R_FIX_cos_int16(x);
```
3.2.6 Arc tangent Function

[Interface] int16 R_FIX_atan_int16(int16_t x)

[Description] Computes the principal of arc tangent. The result is radian value.

[Header] "r_fixmath.h"

[Return Value] Result of arc tangent (in radian),
where 0 <= R_FIX_atan_int16(x) < 0x2000 (corresponding to pi/4).

[Parameters] x: integer, where 0 <= x <= 255

[Example] #include "r_fixmath.h"
Int16_t x, ret;

ret = R_FIX_atan_int16(x);
3.2.7 Arc tangent Function of two variables

[Interface] int16 R_FIX_atan2_int16(int16_t x, int16_t y)

[Description] Computes the principal value of the arc tangent of y/x. The result is radian value.

[Header] "r_fixmath.h"

[Return Value] Result of arctangent (in radian),
where -2048 <= R_FIX_atan2_int16(x, y) <= 2048 (corresponding to pi).
The following are the return value of singular point:

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
<th>Return value</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>+</td>
<td>1024</td>
</tr>
<tr>
<td>0</td>
<td>-</td>
<td>-1024</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>512</td>
</tr>
<tr>
<td>+</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>-</td>
<td>0</td>
<td>-2048</td>
</tr>
</tbody>
</table>

[Parameters] x: integer

[Example] #include "r_fixmath.h"
Int16_t x, y, ret;

    ret = R_FIX_atan2_int16(x, y);
3.2.8 Square Root Function

[Interface] uint16_t R_FIX_sqrt_int16(uint16_t x)

[Description] Computes the square root of FIX12 fixed-point data “ax”.

[Header] "fixmath.h"

[Return Value] Result of square root of ax in FIX12 format. Its range is [0, 16383].

[Parameters] x: FIX12 fixed-point data.

[Example]
#include "fixmath.h"
FIX12 x, ret;
ret = (FIX12)R_FIX_sqrt_int16((uint16_t)x);

3.2.9 Square Root of sum of squares

[Interface] uint16_t R_FIX_sqrt2_int16(int16_t x, int16_t y)

[Description] Computes the square root of x^2 + y^2.

[Header] "fixmath.h"

[Return Value] Result of square root of ax in FIX12 format. Its range is [0, 16383].

[Parameters] x: FIX12 fixed-point data.
y: FIX12 fixed-point data.

[Example]
#include "fixmath.h"
FIX12 x, y, ret;
ret = (FIX12)R_FIX_sqrt2_int16(x, y);
3.2.10 Limit Function

(1) Limit function

[Interface] int16_t R_FIX_limit_int16(int16_t x, uint16_t limit)

[Description] Computes the limited value of given data “x”.

[Header] "fixmath.h"

[Return Value] Result of the limited value. Its range is [-limit, limit].

[Parameters] x: 16-bit integer data to be limited.
limit: limit value at positive side.

[Example]
#include "fixmath.h"
int16_t x, ret;
ret = R_FIX_limit_int16(x, 4096U);

(2) Limit function greater than equal to zero

[Interface] uint16_t R_FIX_ulimit_int16(int16_t x, uint16_t limit)

[Description] Computes the limited value of given data “x”. The result is greater than equal to 0.

[Header] "fixmath.h"

[Return Value] Result of the limited value. Its range is [0, limit].

[Parameters] x: 16-bit integer data to be limited.
limit: limit value at positive side.

[Example]
#include "fixmath.h"
int16_t x;
uint16_t ret;
ret = R_FIX_ulimit_int16 (x, 4096U);
4. Specification of Motor Fixed-point Library

4.1 “r_dsp.h”

This header file defines types and functions for motor control and fix point operations.

The motor control functions declared are listed in table 9.

<table>
<thead>
<tr>
<th>Category</th>
<th>Name</th>
<th>Parameter Type</th>
<th>Return Type</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clarke</td>
<td>R_motor_uvw2ab_int16</td>
<td>int16_t, u, v, w, int16_t *a, int16_t *b</td>
<td>None</td>
<td>3-axis stationary frame to 2-axis stationary frame transform</td>
</tr>
<tr>
<td>Clarke</td>
<td>R_motor_uw2ab_int16</td>
<td>int16_t, u, w, int16_t *a, int16_t *b</td>
<td>None</td>
<td>3-axis stationary frame to 2-axis stationary frame transform. (Equation used when v =1 - u - w is considered)</td>
</tr>
<tr>
<td>Clarke</td>
<td>R_motor_uv2ab_int16</td>
<td>int16_t, u, v, int16_t *a, int16_t *b</td>
<td>None</td>
<td>3-axis stationary frame to 2-axis stationary frame transform. (Equation used when w =1 - u - v is considered)</td>
</tr>
<tr>
<td>Inverse</td>
<td>R_motor_ab2uvw_int16</td>
<td>int16_t, a, b, u, v, w</td>
<td>None</td>
<td>2-axis stationary frame to 3-axis stationary frame transform</td>
</tr>
<tr>
<td>Park</td>
<td>R_motor_ab2dq_int16</td>
<td>int16_t, a, b, wt, d, q</td>
<td>None</td>
<td>2-axis stationary frame to 2-axis rotating frame transform</td>
</tr>
<tr>
<td>Inverse</td>
<td>R_motor_dq2ab_int16</td>
<td>int16_t, d, q, wt, d, a, int16_t *b</td>
<td>None</td>
<td>2-axis rotating frame to 2-axis stationary frame transform</td>
</tr>
<tr>
<td>Coordinate Transform</td>
<td>R_motor_xy2ra_int16*</td>
<td>int16_t, x, y, r, a</td>
<td>None</td>
<td>Orthogonal coordinate to rotation coordinate transform.</td>
</tr>
<tr>
<td>Coordinate Transform</td>
<td>R_motor_ra2xy_int16*</td>
<td>int16_t, r, a, x, y</td>
<td>None</td>
<td>Rotation coordinate to orthogonal coordinate transform</td>
</tr>
<tr>
<td>PID</td>
<td>R_motor_PI_int16</td>
<td>int16_t, err, max, kp, ki, int32_t *integ</td>
<td>None</td>
<td>PI Controller</td>
</tr>
</tbody>
</table>
4.2 Function Specifications

4.2.1 R_motor_uvw2ab_int16

[Interface]  void R_motor_uvw2ab_int16(int16_t u, int16_t v, int16_t w, int16_t *a, int16_t *b)

[Description]  3-axis stationary frame to 2-axis stationary frame transform. The equation is as follows.

\[
\begin{bmatrix}
\alpha \\
\beta
\end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix}
1 & -1/2 & -1/2 \\
0 & \sqrt{3}/2 & -\sqrt{3}/2
\end{bmatrix} \begin{bmatrix}
u \\
v \\
w
\end{bmatrix}
\]

[Header]  “r_dsp.h”

[Return Value]  None.

[Parameters]  
- u: integer, where -16384 <= u <= 16383
- v: integer, where -16384 <= v <= 16383
- w: integer, where -16384 <= w <= 16383
- *a: integer, where |*a| < sqrt(2/3) * 32768
- *b: integer, where |*b| < sqrt(1/2) * 32768

[Example]  
```
#include "r_dsp.h"

int16_t u, v, w, a, b;

R_motor_uvw2ab_int16(u, v, w, &a, &b);
```
4.2.2 R_motor_uw2ab_int16

[Interface] void R_motor_uw2ab_int16 (int16_t u, int16_t w, int16_t *a, int16_t *b )

[Description] 3-axis stationary frame to 2-axis stationary frame transform. The equation is as follows.

\[
\begin{bmatrix}
\alpha \\
\beta
\end{bmatrix} = \begin{bmatrix}
\frac{\sqrt{3}}{2} & 0 \\
-\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2}
\end{bmatrix} \begin{bmatrix}
u \\
w
\end{bmatrix}
\]

[Header] “r_dsp.h”

[Return Value] None.

[Parameters] u: integer, where -10922 <= u <= 10922
w: integer, where -10922 <= w <= 10922
*a: integer, where |*a| < sqrt(2/3) * 32768
*b: integer, where |*b| < sqrt(1/2) * 32768

[Example] #include "r_dsp.h"
int16_t u, w, a, b;
R_motor_uw2ab_int16(u, w, &a, &b);
4.2.3 R_motor_uv2ab_int16

[Interface] void R_motor_uv2ab_int16 (int16_t u, int16_t v, int16_t *a, int16_t *b)

[Description] 3-axis stationary frame to 2-axis stationary frame transform. The equation is as follows.

\[
\begin{bmatrix}
\alpha \\
\beta \\
\end{bmatrix} = 
\begin{bmatrix}
\frac{\sqrt{3}}{2} & 0 \\
\frac{\sqrt{1}}{2} & \frac{\sqrt{2}}{2}
\end{bmatrix}
\begin{bmatrix}
u \\
v
\end{bmatrix}
\]

[Header] “r_dsp.h”

[Return Value] None.

[Parameters]  
u: integer, where -10922 <= u <= 10922  
v: integer, where -10922 <= v <= 10922  
*a: integer, where |*a| < sqrt(2/3) * 32768  
*b: integer, where |*b| < sqrt(1/2) * 32768

[Example] 

```c
#include "r_dsp.h"

int16_t u, v, a, b;

R_motor_uv2ab_int16(u, v, &a, &b);
```
4.2.4 R_motor_ab2uvw_int16

[Interface]  void R_motor_ab2uvw_int16 (int16_t a, int16_t b, int16_t *u, int16_t *v, int16_t *w)

[Description] 2-axis stationary frame to 3-axis stationary frame transform. The equation is as follows.

\[
\begin{bmatrix}
  u \\
  v \\
  w
\end{bmatrix} = \begin{bmatrix}
  1 & 0 \\
  -1/2 & \sqrt{3}/2 \\
  -1/2 & -\sqrt{3}/2
\end{bmatrix} \begin{bmatrix}
  \alpha \\
  \beta
\end{bmatrix}
\]

[Header]  “r_dsp.h”

[Return Value]  None.

[Parameters]  
- a: integer, where -32768 <= a <= 32767
- b: integer, where -32768 <= b <= 32767
- *u: integer, where |*u| < sqrt(2/3) * 32768
- *v: integer, where |*v| < sqrt(1/2) * 32768
- *w: integer, where |*w| < sqrt(1/2) * 32768

[Example]  
```
#include "r_dsp.h"

int16_t u, v, w, a, b;

R_motor_ab2uvw_int16(a, b, &u, &v, &w);
```
4.2.5 R_motor_ab2dq_int16

[Interface] void R_motor_ab2dq_int16 (int16_t a, int16_t b, int16_t wt, int16_t *d, int16_t *q)

[Description] 2-axis stationary frame to 2-axis rotating frame transform. The equation is as follows.

\[
\begin{bmatrix}
    d \\
    q
\end{bmatrix}
= 
\begin{bmatrix}
    \cos \omega t & \sin \omega t \\
    -\sin \omega t & \cos \omega t
\end{bmatrix}
\begin{bmatrix}
    \alpha \\
    \beta
\end{bmatrix}
\]

[Header] “r_dsp.h”

[Return Value] None.

[Parameters] a: integer, where -23168 <= a <= 23168
b: integer, where -23168 <= b <= 23168
wt: integer, where -32768 <= wt <= 32767, wt is a parameter that performs arithmetic operations
\(2 \pi = 4096\).
*d: integer, where -32768 <= *d <= 32767
*q: integer, where -32768 <= *q <= 32767

[Example] #include "r_dsp.h"
int16_t a, b, wt, d, q;

    R_motor_ab2dq_int16(a, b, wt, &d, &q);
4.2.6  R_motor_dq2ab_int16

**[Interface]**

```c
void R_motor_dq2ab_int16 (int16_t d, int16_t q, int16_t wt, int16_t *a, int16_t *b)
```

**[Description]** 2-axis rotating frame to 2-axis stationary frame transform. The equation is as follows.

$$
\begin{bmatrix}
\alpha \\
\beta 
\end{bmatrix} =
\begin{bmatrix}
\cos \omega t & -\sin \omega t \\
\sin \omega t & \cos \omega t 
\end{bmatrix}
\begin{bmatrix}
d \\
q 
\end{bmatrix}
$$

**[Header]** “r_dsp.h”

**[Return Value]** None.

**[Parameters]**

d: integer, where -16384 <= d <= 16383
q: integer, where -16384 <= q <= 16383
wt: integer, where -32768 <= wt <= 32767, wt is a parameter that performs arithmetic operations
\(2\pi = 4096\).
*a*: integer, where -32768 <= *a* <= 32767
*b*: integer, where -32768 <= *b* <= 32767

**[Example]**

```c
#include "r_dsp.h"

int16_t a, b, wt, d, q;

R_motor_dq2ab_int16(d, q, wt, &a, &b);
```
4.2.7 R_motor_xy2ra_int16

[Interface] void R_motor_xy2ab_int16 (int16_t x, int16_t y, int16_t *r, int16_t *a)

[Description] Orthogonal coordinate to rotation coordinate transform. The equation is as follows.

\[
\begin{align*}
    r &= \sqrt{x^2 + y^2} \\
    \alpha &= \tan^{-1} \left( \frac{y}{x} \right)
\end{align*}
\]

[Header] “r_dsp.h”

[Return Value] None.

[Parameters]
- x: integer, where -16384 <= x <= 16383
- y: integer, where -16384 <= y <= 16383
- *r: integer, where -32768 <= *r <= 32767
- *a: integer, where -2048 <= *a <= 2047, *a is a parameter that performs arithmetic operations \(\pi = 4096\).

[Example]
```c
#include "r_dsp.h"
int16_t x, y, r, a;
R_motor_xy2ab_int16(x, y, &r, &a);
```
4.2.8 R_motor_ra2xy_int16

[Interface] void R_motor_ra2xy_int16 (int16_t r, int16_t a, int16_t *x, int16_t *y)

[Description] Rotation coordinate to orthogonal coordinate transform. The equation is as follows.

\[
\begin{align*}
  x &= r \cos \alpha \\
  y &= r \sin \alpha 
\end{align*}
\]

[Header] “r_dsp.h”

[Return Value] None.

[Parameters] r: integer, where -32768 <= r <= 32767
a: integer, where -32768 <= a <= 32767
*x: integer, where -32768 <= *x <= 32767
*y: integer, where -32768 <= *y <= 32767

[Example] #include "r_dsp.h"
int16_t x, y, r, a;

R_motor_ra2xy_int16(r, a, &x, &y);
4.2.9 R_motor_PI_int16

**[Interface]** int16_t void R_motor_PI_int16 (int16_t err, int16_t max, int16_t kp, int16_t ki, int16_t *integ)

**[Description]** The block diagram of PI controller.

∑ 

\[ P \frac{K_e}{r(t)} \]

∑ 

\[ I \frac{\int K_e r(t) dt}{r} \]

Clamp

**[Header]** “r_dsp.h”

**[Return Value]** None.

**[Parameters]**
- err: integer, where \(-32768 \leq err \leq 32767\)
- max: integer, where \(0 \leq max \leq 32767\)
- kp: integer, where \(-32768 \leq kp \leq 32767\)
- ki: integer, where \(-32768 \leq ki \leq 32767\)
- *integ: integer, where \(-max \leq *integ \leq max\)

**[Example]**
```c
#include "r_dsp.h"
int16_t err, max, kp, ki, integral;

R_motor_PI_int16(err, max, kp, ki, &integral);
```
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## Revision Record

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<th>Rev.</th>
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<tr>
<td>1.00</td>
<td>Jun.15.12</td>
<td>—</td>
<td>First edition issued</td>
</tr>
<tr>
<td>1.01</td>
<td>Jun.10.13</td>
<td>—</td>
<td>Workspace's DSC Library updated to accommodate all RL78/G14 devices</td>
</tr>
</tbody>
</table>
General Precautions in the Handling of MPU/MCU Products

The following usage notes are applicable to all MPU/MCU products from Renesas. For detailed usage notes on the products covered by this manual, refer to the relevant sections of the manual. If the descriptions under General Precautions in the Handling of MPU/MCU Products and in the body of the manual differ from each other, the description in the body of the manual takes precedence.

<table>
<thead>
<tr>
<th>1. Handling of Unused Pins</th>
</tr>
</thead>
<tbody>
<tr>
<td>Handle unused pins in accord with the directions given under Handling of Unused Pins in the manual.</td>
</tr>
<tr>
<td>— The input pins of CMOS products are generally in the high-impedance state. In operation with an unused pin in the open-circuit state, extra electromagnetic noise is induced in the vicinity of LSI, an associated shoot-through current flows internally, and malfunctions occur due to the false recognition of the pin state as an input signal become possible. Unused pins should be handled as described under Handling of Unused Pins in the manual.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>2. Processing at Power-on</th>
</tr>
</thead>
<tbody>
<tr>
<td>The state of the product is undefined at the moment when power is supplied.</td>
</tr>
<tr>
<td>— The states of internal circuits in the LSI are indeterminate and the states of register settings and pins are undefined at the moment when power is supplied.</td>
</tr>
<tr>
<td>In a finished product where the reset signal is applied to the external reset pin, the states of pins are not guaranteed from the moment when power is supplied until the reset process is completed.</td>
</tr>
<tr>
<td>In a similar way, the states of pins in a product that is reset by an on-chip power-on reset function are not guaranteed from the moment when power is supplied until the power reaches the level at which resetting has been specified.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>3. Prohibition of Access to Reserved Addresses</th>
</tr>
</thead>
<tbody>
<tr>
<td>Access to reserved addresses is prohibited.</td>
</tr>
<tr>
<td>— The reserved addresses are provided for the possible future expansion of functions. Do not access these addresses; the correct operation of LSI is not guaranteed if they are accessed.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>4. Clock Signals</th>
</tr>
</thead>
<tbody>
<tr>
<td>After applying a reset, only release the reset line after the operating clock signal has become stable.</td>
</tr>
<tr>
<td>When switching the clock signal during program execution, wait until the target clock signal has stabilized.</td>
</tr>
<tr>
<td>— When the clock signal is generated with an external resonator (or from an external oscillator) during a reset, ensure that the reset line is only released after full stabilization of the clock signal. Moreover, when switching to a clock signal produced with an external resonator (or by an external oscillator) while program execution is in progress, wait until the target clock signal is stable.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>5. Differences between Products</th>
</tr>
</thead>
<tbody>
<tr>
<td>Before changing from one product to another, i.e. to one with a different type number, confirm that the change will not lead to problems.</td>
</tr>
<tr>
<td>— The characteristics of MPU/MCU in the same group but having different type numbers may differ because of the differences in internal memory capacity and layout pattern. When changing to products of different type numbers, implement a system-evaluation test for each of the products.</td>
</tr>
</tbody>
</table>
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